

FACTORING TRINOMIALS

learning goals

- new vocabulary
- demonstrate the difference in processes required in factoring
- factor effectively

Recall:

Common Factoring - divide the same thing out of each term

ex. $6a+18$

$$= 6(a+3)$$

ex. $6a^5-12a^3$

$$= 6a^3(1a^2-2)$$

Difference of Squares - two perfect squares that are subtracted from each other

ex. a^2-9

$$= (a+3)(a-3)$$

ex. $4a^2-16b^2$

$$= 4(a^2-4b^2)$$
$$= 4(a+2b)(a-2b)$$

On the Boards...

Factor.

(a) $2x + 8$

(e) $2a - 4b + 8c$

(b) $15m^2 - 5m$

(f) $5x + 10x^2 + 15$

(c) $4a^2 - 8a$

(g) $6a^2 + 12a^3 + 2a$

EXPANDING - getting rid of brackets by multiplication

$$\begin{aligned}
 (x+3)(x+2) &= x^2 + 3x + 2x + 6 \\
 &= x^2 + 5x + 6
 \end{aligned}$$

FACTORING - adding in brackets by division

$$x^2 + 5x + 6 = (x + 3)(x + 2)$$

The two processes are opposite of one another.

EXPAND (x)

$$(x+2)(x+3) = x^2 + 5x + 6$$

FACTOR (÷)

Factoring Trinomials of the

Form $\overset{1}{\downarrow} x^2 + bx + c$

$$x^2 + 6x + 8$$

$$\underline{2} \times \underline{4} = 8$$

$$\underline{2} + \underline{4} = 6$$

$$= (x + 2)(x + 4)$$

Steps:

1. Put terms in order

2. Look for 2 numbers

$$\underline{\quad} \times \underline{\quad} = \text{last}$$

$$\underline{\quad} + \underline{\quad} = \text{middle}$$

$$9x + 20 + x^2$$

$$= x^2 + 9x + 20$$

$$\underline{5} \times \underline{4} = 20$$

$$= (x + 5)(x + 4)$$

$$\underline{5} + \underline{4} = 9$$

Find the dimensions of a rectangle with the given area

length
width

a. $A = 24 \text{ cm}^2$

$$A = lw$$

$$24 = lw$$

$$3, 8$$

$$2, 12$$

$$1, 24$$

$$4, 6$$

b. $A = x^2 + x - 12$

$$\underline{4} \times \underline{-3} = -12$$

$$\underline{4} + \underline{-3} = 1$$

$$= (x + 4)(x - 3)$$

On the Boards...

$$1. \quad x^2 - 3x - 18 = (x - 6)(x + 3)$$

$$2. \quad x^2 + 2x - 35 = (x + 7)(x - 5)$$

$$3. \quad x^2 - 12x + 36 = (x - 6)(x - 6)$$

$$4. \quad x^2 + 7xy - 18y^2 = (x - 2y)(x + 9y)$$

The area of a rectangular garden can be represented by the expression $x^2 + 7x + 10$.

- a) Find expressions for the length and width of the garden.
~~b) If the area is 40 m^2 , find the length and width.~~

$$a. \quad (x + 2)(x + 5)$$

Homework

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